

# From Network Interface to Multithreaded Web Applications: A Case Study in Modular Program Verification

Adam Chlipala – MIT CSAIL  
POPL 2015  
January 17, 2015

# Whole Program

Application

Proof

.....

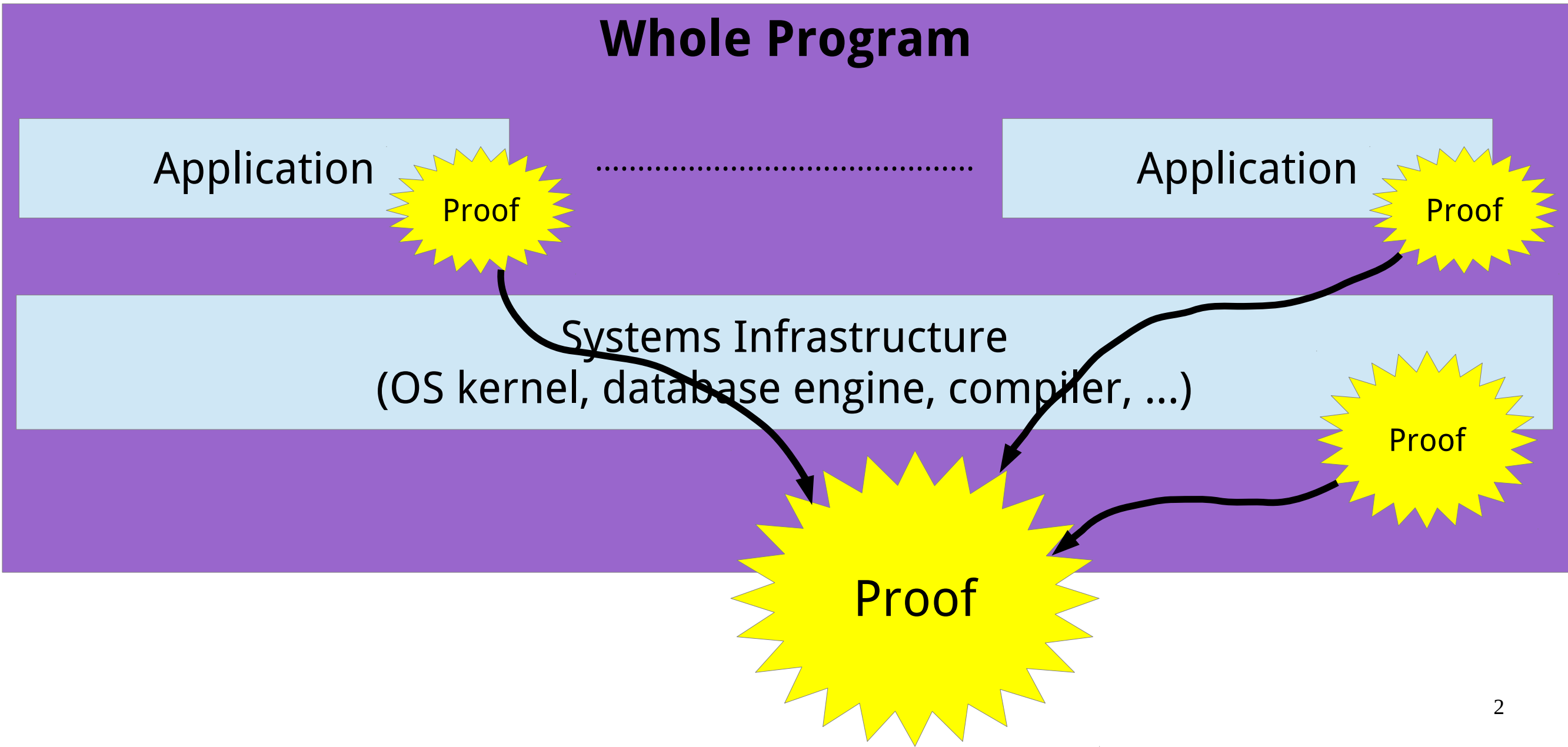
Application

Proof

Systems Infrastructure  
(OS kernel, database engine, compiler, ...)

Proof

Proof



# Whole Program

Application

Proof

.....

Application

Proof

## Systems Infrastructure

Memory Management

Proof

Thread Management

Proof

Blocking IO

Proof

Thread Queues

Proof

Queues

Proof

Proof

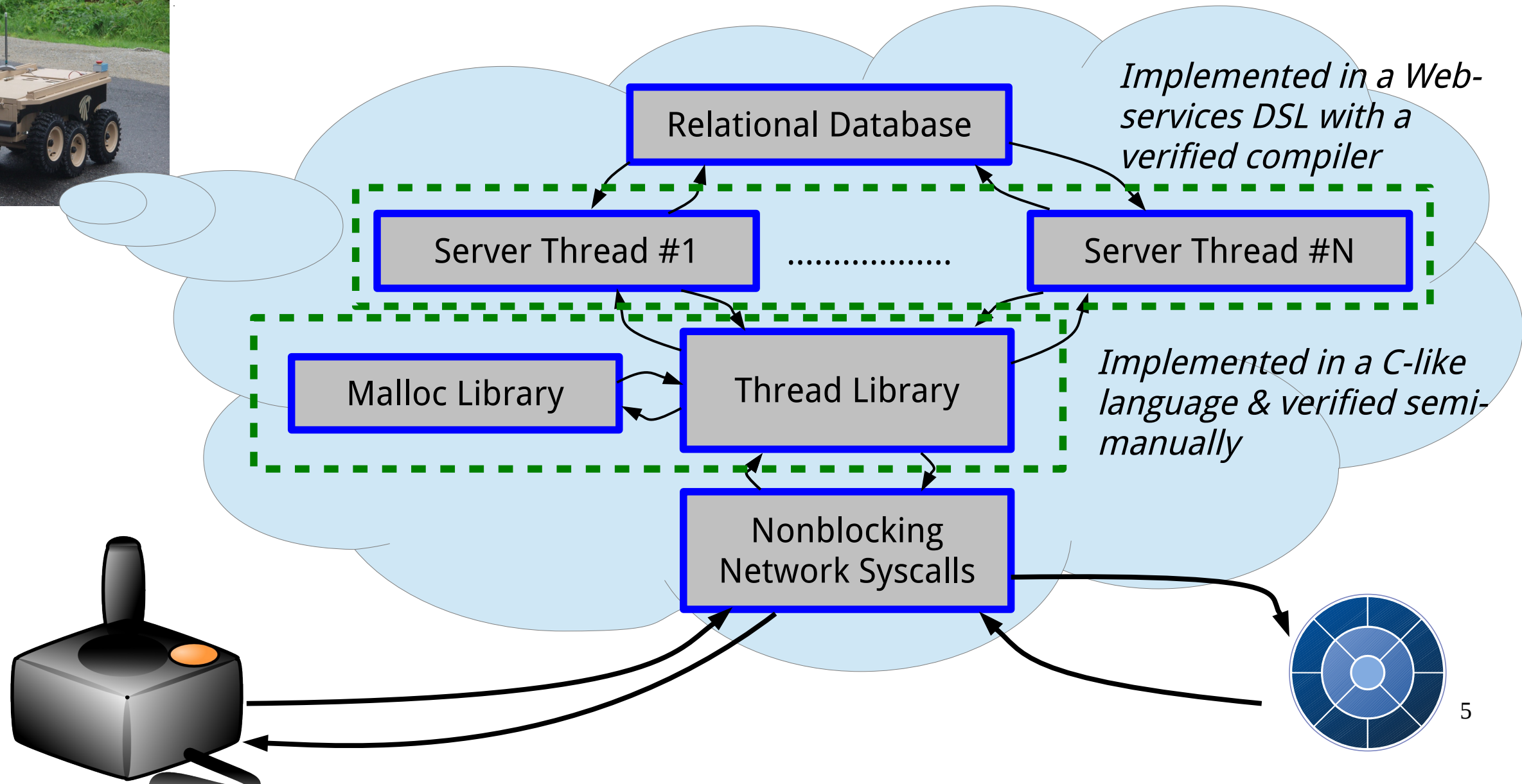
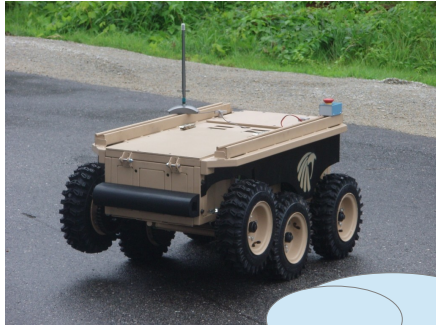
Surprisingly few systems-verification projects have used their results to connect to proofs of applications that someone is actually running.

The modular style also doesn't seem to have been used previously to verify infrastructure serious enough to connect to real applications.

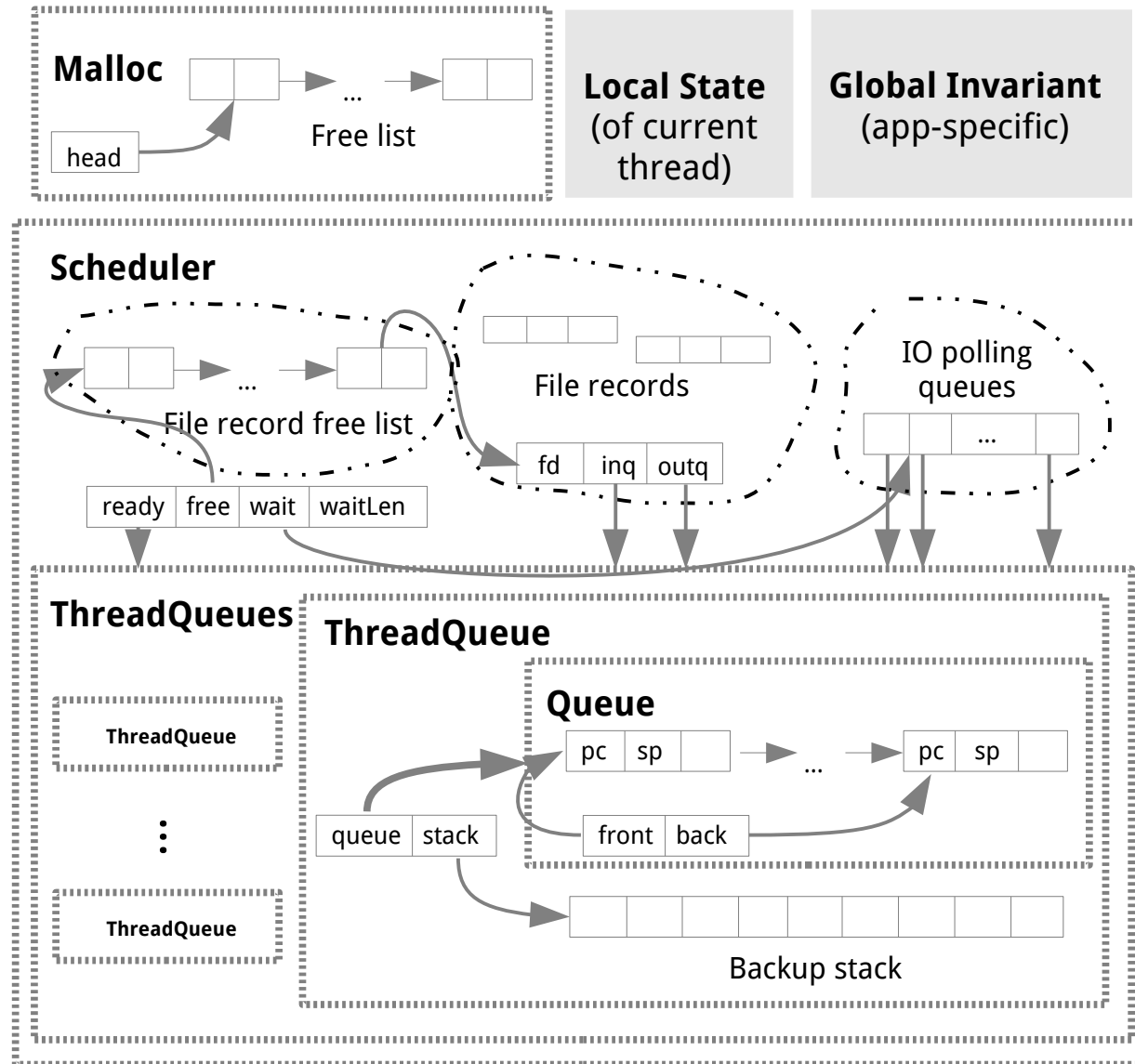
The word "Bedrock" is rendered in a large, 3D, italicized serif font. The letters have a metallic, marbled texture with shades of grey, blue, and green, giving it a rugged, stone-like appearance.

This talk: a case study doing all of the above inside **Coq**, using the **Bedrock** framework

# Deployed on Autonomous Vehicles

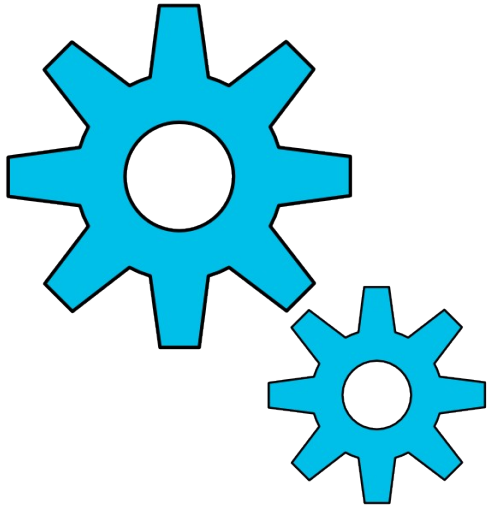


# Example Module Decomposition: Nested Threading Abstractions



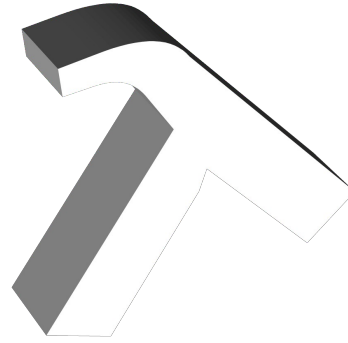
# Plan for Rest of Talk

- Basic stage-setting about this style of verification
- Fundamentals of the Bedrock framework
- Adapting to interface with unverified code in a principled way
- Three “design patterns” of general interest
  - Recursive definitions of higher-order, stateful predicates
  - Good formal interfaces for threading components
  - Modular verification of DSL compilers
- Code & performance



## Highly Automated:

Tools should fill in most of the boring details of proofs.



## Higher-Order:

Can use higher-order logic to state elegant & general specs.

The approach in this case study starts from separation-logic tools of past work (PLDI 2011, ITP 2014) and adds a few new tricks, while also applying them on a much larger scale than before.

## Foundational:

Verification leads to a proof checked by a general-purpose proof assistant (*Coq*, in this case).

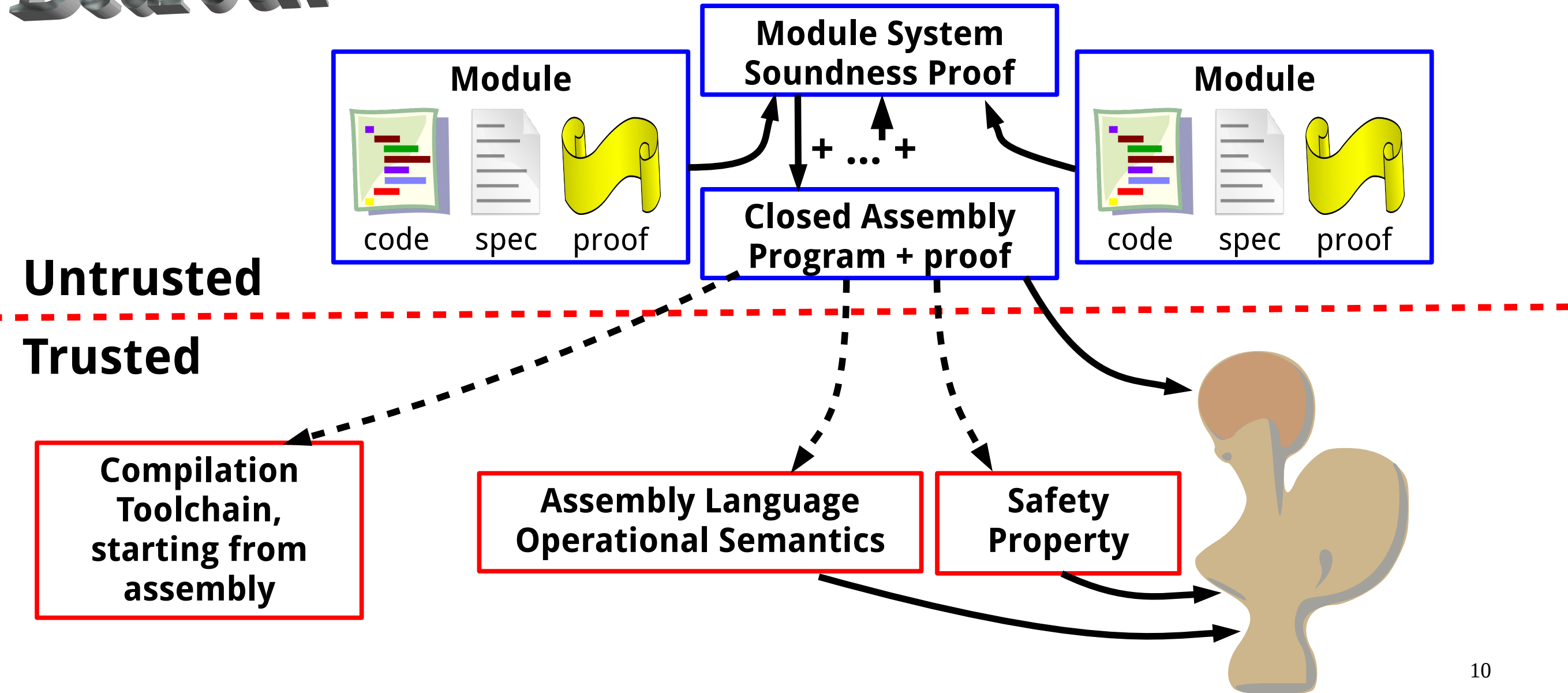
*Trusted code base* includes just the *proof assistant*, operational semantics of *assembly language*, and a *specification* for the whole program.



# Inventory of Corners Cut

- Proving functional correctness for systems code, but only data-structure shape invariants for application.
- Performance of verified server is OK, but it's not hard to do better. (Some parts simplified to make proofs easier.)
- Level of proof automation varies across components. Some proofs are fairly manual. (Overall proof-to-program ratio [ $\sim 5:1$ ] remains well below those reported in related projects [ $\geq 20:1$ ].)

## What Should We Trust?



# Bedrock version of linked list length

Specification

```
Definition lengthS : spec := SPEC("x") reserving 1
  All ls,
  PRE[V] sll ls (V "x")
  POST[R] [| R = length ls |] * sll ls (V "x").
```

Implementation

```
bfunction "length"("x", "n") [lengthS]
  "n" <- 0;;
  [All ls,
    PRE[V] sll ls (V "x")
    POST[R] [| R = V "n" ^+ length ls |] * sll ls (V "x")]
```

Loop invariant

```
  While ("x" <> 0) {
    "n" <- "n" + 1;;
    "x" <-* "x" + 4
  };;
  Return "n"
end.
```

This is all Coq code, taking advantage of Coq's extensible parser!

Proof

```
Theorem sllMok : moduleOk sllM.
Proof.
  vcgen; abstract (sep hints; finish).
Qed.
```

# Now Application Code Looks Like:

```
RosCommand "setParam"(!string $"caller_id",  
                      !string $"key", !any $$"value")
```

Program defines  
**remote procedure  
call** entry points.

Do

```
Delete "params" Where ("key" = $"key");;  
Insert "params" ($"key", $"value");;
```

Manipulates  
**relational database**  
(simple updates and  
queries).

```
From "paramSubscribers" Where ("key" = $"key") Do  
  Callback "paramSubscribers#"subscriber_api"  
  Command "paramUpdate"(!string "/master", !string $"key", $"value");;
```

**Response** Success

Message "Parameter set."

Body ignore

end

end

**Callbacks** trigger calls  
to similar functions on  
other nodes.  
**XML pattern-matching and generation**  
(Network communication is all via XML over HTTP.)

```
Theorem Wf : wf ts pr buf_size outbuf_size.
```

```
Proof.
```

```
  wf.
```

```
Qed.
```

**Automatic well-formedness  
proof** establishes assumption  
of *verified compiler*.

# Connecting with Untrusted Support Code

We assume that the following *nonblocking system calls* exist, abstracting a TCP/IP network interface:

```
// Standard TCP socket operations
fd_t listen(int port);
fd_t accept(fd_t sock);
int read(fd_t sock, void *buf, int n_bytes);
int write(fd_t sock, void *buf, int n_bytes);
void close(fd_t sock);

// epoll-style IO event notification
res_t declare(fd_t sock, bool isWrite);
res_t wait(bool isBlocking);
```

# Add System Calls to Operational Semantics

$$\frac{\begin{array}{l} [r.Sp, r.Sp + 16) \in \text{ValidMem} \\ m[r.Sp + 8] = \text{buf} \\ m[r.Sp + 12] = \text{len} \\ [buf, buf + len) \in \text{ValidMem} \\ r'.Sp = r.Sp \\ \forall a. a \notin [buf, buf + len) \rightarrow m'[a] = m[a] \end{array}}{(m, \text{read}, r) \rightarrow (m', r.Rp, r')}$$

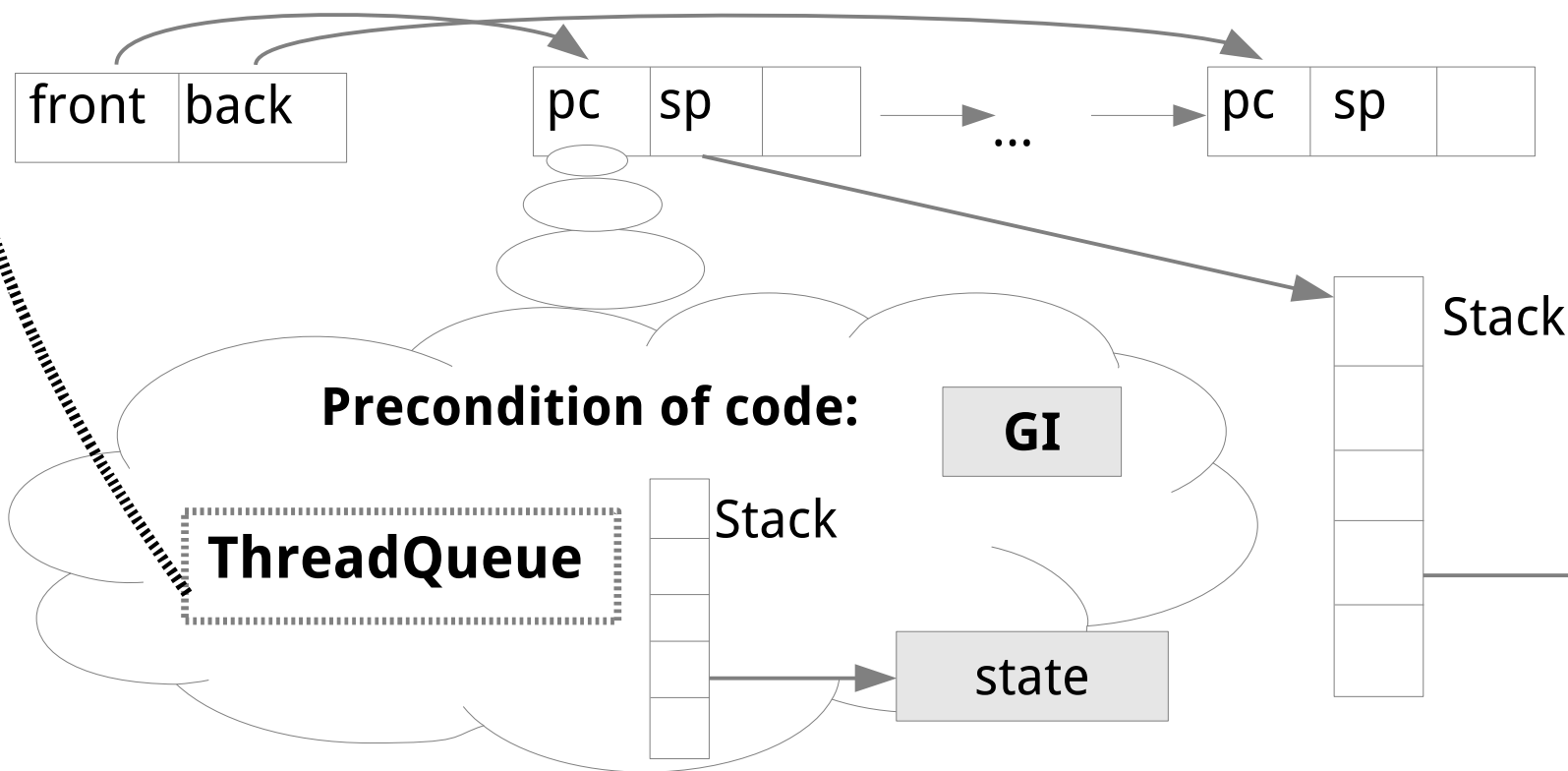
Each op. sem. rule has a corresponding **separation logic** rule, proved sound w.r.t. the original. E.g.:

$$\frac{\{buf \overset{?}{\rightarrow} len\}}{\text{read(sock, buf, len)} \{buf \overset{?}{\rightarrow} len\}}$$

State: (memory, program counter, registers)

# Recursive, Higher-Order, Stateful Predicates

## ThreadQueue



**Global Invariant:**  
Application-specific  
and seen by all  
threads

Other thread-local  
state

# A Simpler Case

Watch out for recursive predicate definitions that are **inconsistent** when interpreted naively! E.g.:

$$P(p) \stackrel{\text{def}}{=} \exists q. p \rightarrow 42, q \wedge \{P(p)\} q \{P(p)\}$$

$$P(p) \stackrel{\text{def}}{=} \mu\rho. \exists q. p \rightarrow 42, \text{and } \rho$$

$$P(p) \stackrel{\text{def}}{=} \exists q. p \rightarrow 42, \text{and } \text{recOf}("P")(p)\}$$

Allow code modules to come packaged with **named predicate definitions**, which can be looked up within specs. Now the funky reasoning only applies when we reason about the higher-order parts of a definition.

Bravely going ahead with *general-recursive predicates*! Requires restrictive **side conditions** throughout proofs, to avoid inconsistency.

*See paper for:* a cute trick to encode named predicates as named functions in the code to verify.

# Specifying a Thread Stack

## **ThreadQueue** module

Parameters: a set of **worlds**, a **global invariant** ginv in terms of it, and an **evolution relation**  $\preceq$

$$\begin{aligned} & \forall w. \{ \text{tq}(w, q) * \text{ginv}(w, q) \} \\ & \quad \text{yield}(q) \\ & \{ \exists w'. w \preceq w' \wedge \text{tq}(w', q) * \text{ginv}(w', q) \} \end{aligned}$$

## **ThreadQueues** module

Parameters: like above, except argument to ginv is *set of queues*, not just one queue

$$\begin{aligned} & \forall w, Q. \{ \text{tqs}(w, Q) * \text{ginv}(w, Q) \wedge \text{inq} \in Q \wedge \text{outq} \in Q \} \\ & \quad \text{yield}(\text{inq}, \text{outq}) \\ & \{ \exists w', Q'. w \preceq w' \wedge Q \subseteq Q' \wedge \text{tqs}(w', Q') * \text{ginv}(w', Q') \} \end{aligned}$$

Use **ThreadQueue** as a submodule by *deriving its parameters from these!*

## **Scheduler** module

Parameters: like above, except argument to ginv is hardcoded as *set of open files*

$$\forall F. \{ \text{sched}(F) * \text{ginv}(F) \} \text{yield}() \{ \exists F'. F \subseteq F' \wedge \text{sched}(F') * \text{ginv}(F') \}$$

## Example verification of a client application (echo server)

```
bfunctionNoRet "handler"("buf", "listener", "accepted", "n", "Sn")
  [handlerS]
  "listener" <-- Call "scheduler"! "listen"(port)
  [Al fs, PREmain[_ , R] [| R %in fs |] * sched fs * mallocHeap 0];;
  "buf" <-- Call "buffers"! "bmalloc"(inbuf_size)
  [Al fs, PREmain[V, R] R =?>8 bsize * [| R <> 0 |] * [| freeable R inbuf_size |] * [| V "listener" %in fs|] * sched fs *
mallocHeap 0];;
  "accepted" <-- Call "scheduler"! "accept"("listener")
  [Al fs, PREmain[V, R] [| R %in fs |] * V "buf" =?>8 bsize * [| V "buf" <> 0 |] * [| freeable (V "buf") inbuf_size |] * [| V
"listener" %in fs|] * sched fs * mallocHeap 0];;
  "n" <-- Call "scheduler"! "read"("accepted", "buf", bsize)
  [Al fs, PREmain[V] [| V "accepted" %in fs |] * V "buf" =?>8 bsize * [| V "buf" <> 0 |] * [| freeable (V "buf") inbuf_size |] *
[| V "listener" %in fs|] * sched fs * mallocHeap 0];;
  "Sn" <- "n" + 1;;
  Call "scheduler"! "close"("accepted")
  [Al fs, PREmain[V] V "buf" =?>8 bsize * [| V "buf" <> 0 |] * [| freeable (V "buf") inbuf_size |] * [| V "listener" %in fs|] *
sched fs * mallocHeap 0 * [| V "Sn" = V "n" ^+ $1 |] ];;
  Call "scheduler"! "close"("listener")
  [Al fs, PREmain[V] V "buf" =?>8 bsize * [| V "buf" <> 0 |] * [| freeable (V "buf") inbuf_size |] * sched fs * mallocHeap 0 * [|
V "Sn" = V "n" ^+ $1 |] ];;
  Call "buffers"! "bfree"("buf", inbuf_size)
  [Al fs, PREmain[V] sched fs * mallocHeap 0 * [| V "Sn" = V "n" ^+ $1 |] ];;
  Call "sys"! "printInt"("Sn")
  [Al fs, PREmain[V] sched fs * mallocHeap 0 * [| V "Sn" = V "n" ^+ $1 |] ];;
  Exit 100
end
```

```
Ltac t := try solve [ sep unf hints; auto ];
  unf; unfold localsInvariantMain; post; evaluate hints; descend;
  try match_locals; sep unf hints; auto.
```

Theorem ok : moduleOk m.

Proof.

vcgen; abstract t.

Qed.

# Modular Verification of a DSL Compiler

Idea: Give a **feature-modular** proof of the DSL compiler.  
Define different language features as standalone **macros** that  
should be usable independently or within other DSLs.

**Legend:**

conventional library

code generator

notations

NumOps

...

ArrayOps

...

[Structure of DSL  
implementation]

XmlLex

StringOps

XmlSearch

XmlOutput

DbCondition

DbSelect

DbInsert

DbDelete

Http

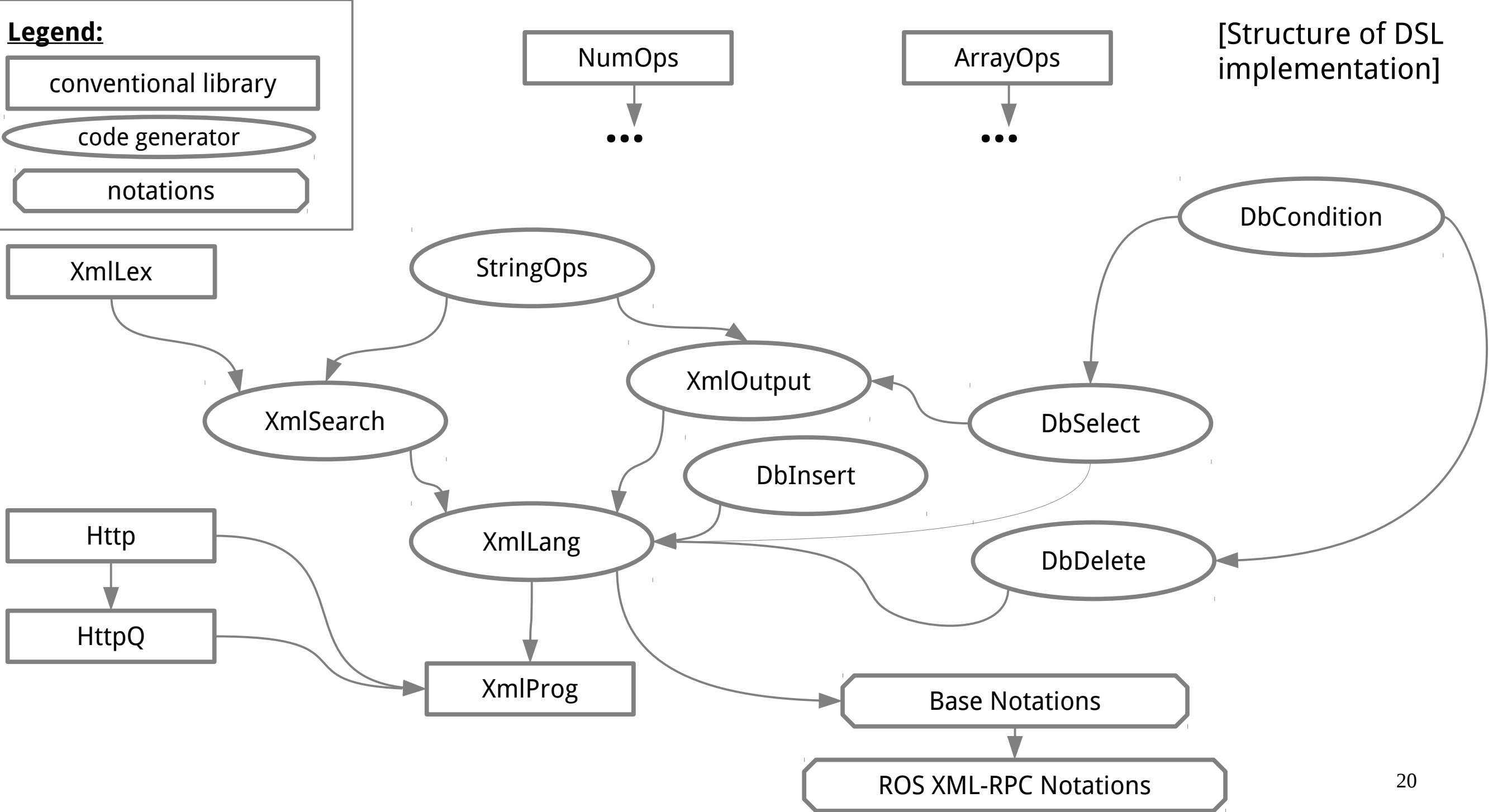
HttpQ

XmlLang

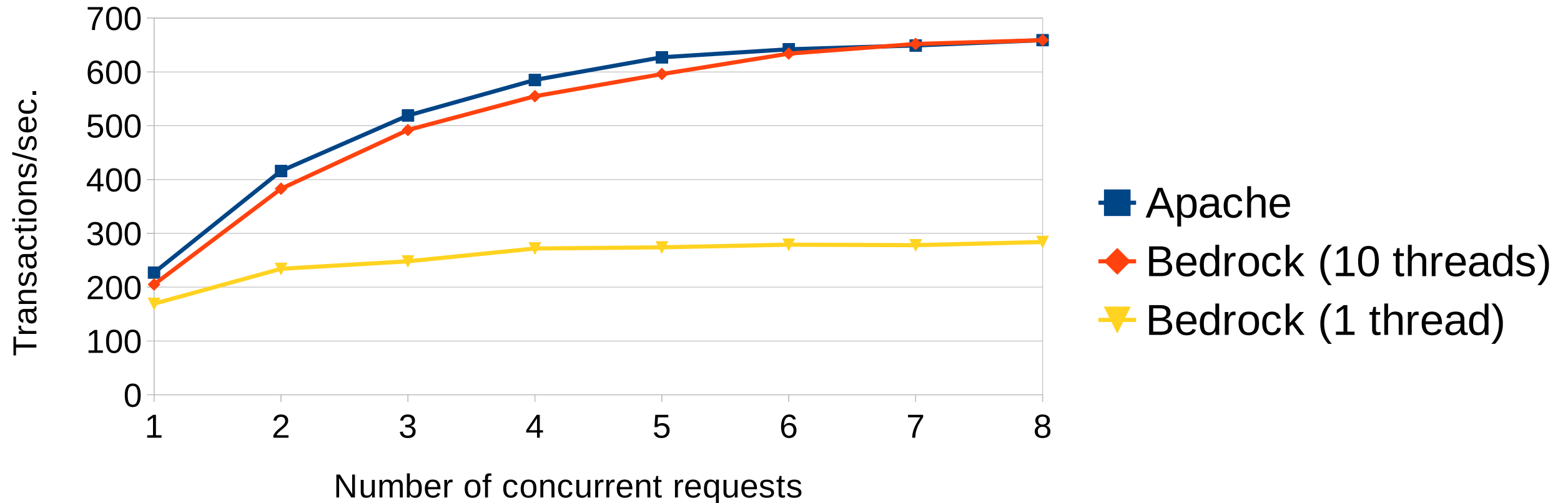
XmlProg

Base Notations

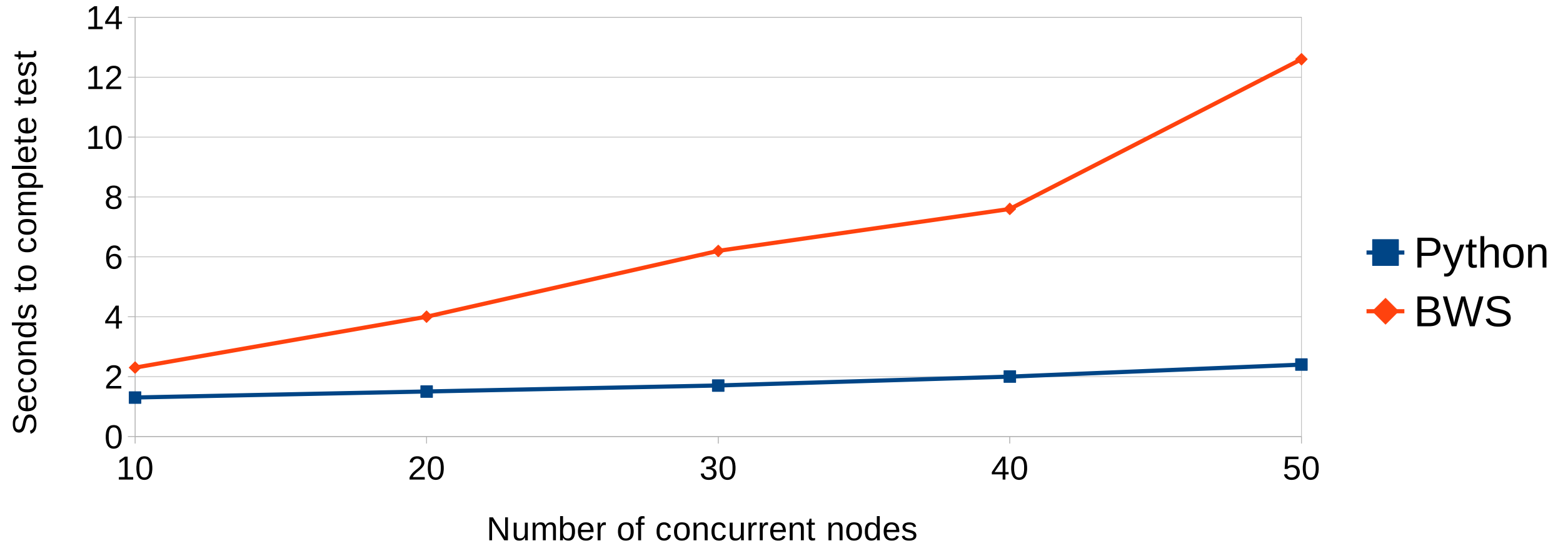
ROS XML-RPC Notations



# Performance Test #1: Static Web Server



# Performance Test #2: Robot Directory Server



# Thanks for listening!

Summary: It is feasible today to verify a usable system including both infrastructure and application code, with a modular reasoning style, mostly automated proofs, and a final theorem checked in Coq with minimal trust dependencies.

Bedrock is on the Web at:

<http://plv.csail.mit.edu/bedrock/>

# Backup Slides

# The Bedrock Intermediate Language

$W ::= (* \text{ width-32 bitvectors } *)$

$L ::= (* \text{ program code block labels } *)$

$\text{Reg} ::= \text{Sp} \mid \text{Rp} \mid \text{Rv}$

$\text{Loc} ::= \text{Reg} \mid W \mid \text{Reg} + W$

$\text{Lvalue} ::= \text{Reg} \mid [\text{Loc}]_{32} \mid [\text{Loc}]_8$

$\text{Rvalue} ::= \text{Lvalue} \mid W \mid L$

$\text{Binop} ::= + \mid - \mid *$

$\text{Test} ::= = \mid != \mid < \mid <=$

$\text{Instr} ::= \text{Lvalue} := \text{Rvalue} \mid \text{Lvalue} := \text{Rvalue Binop Rvalue}$

$\text{Jump} ::= \text{goto Rvalue} \mid \text{if Rvalue Test Rvalue then goto L else goto L}$

$\text{Block} ::= \text{Instr}^*; \text{Jump}$

$\text{Module} ::= (L: \text{Block})^*$

# Verification Foundation: XCAP [Ni & Shao, POPL 2006]

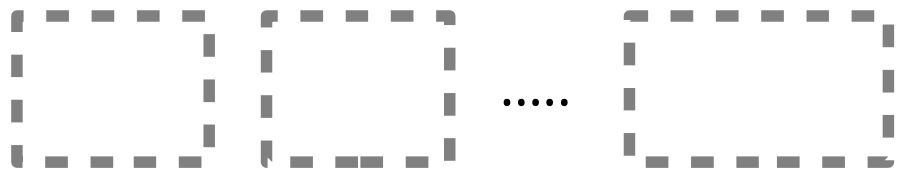
## 1. Whole programs

Basic block

**Precondition**

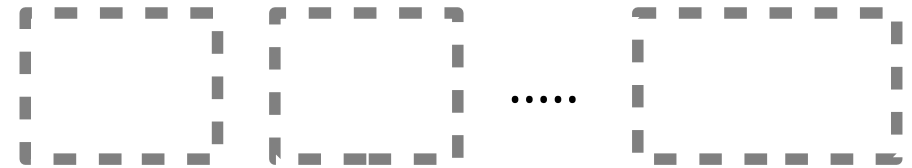
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
jmp \_\_\_\_\_

⋮



## 2. Modules

Code:



Assumptions: {spec1}label1, {spec2}label2, ...

*Correct program.* Proof: Assumptions imply no precondition violations within these blocks.

Each precondition is true each time we reach it.

## 3. Linking

