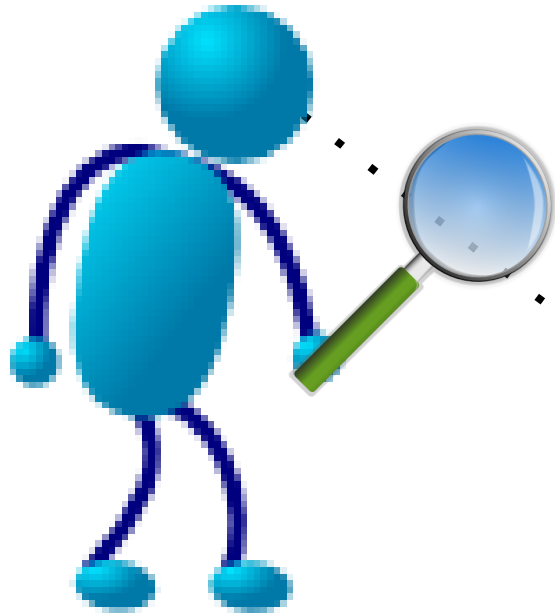


Modular Development of Certified Program Verifiers with a Proof Assistant

Adam Chlipala
University of California, Berkeley
ICFP 2006

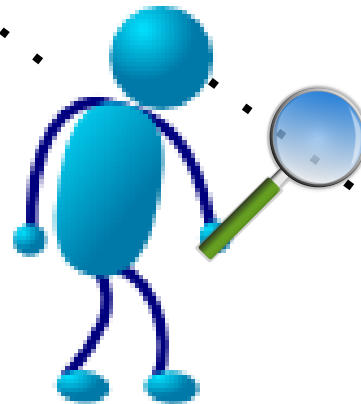
Who Watches the Watcher?



Program Verifier Verifier

- Type-checker for stylized verifier language?
- Result checker on witnesses outputted by verifiers?
- Interactive proof assistant?

Program Verifier



- Java Bytecode Verifier
- Extended Static Checking
- Typed Assembly Language
- Proof-Carrying Code
- Model Checking

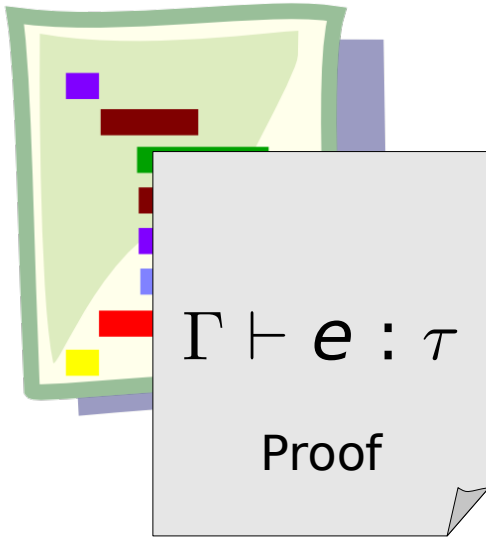
Might want to ensure:

- Memory safety
- Resource usage bounds
- Total correctness



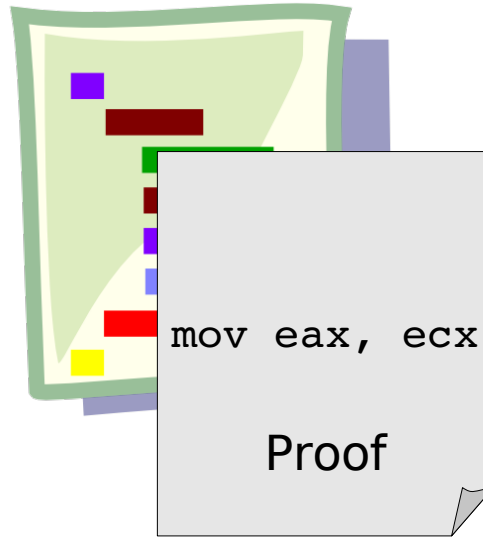
Untrusted Program

But Why?



Proof-Carrying Code

- Compact proofs in a language specialized to one safety mechanism (e.g., a type system)
- Every new safety mechanism requires trusting a new body of code



Foundational Proof-Carrying Code

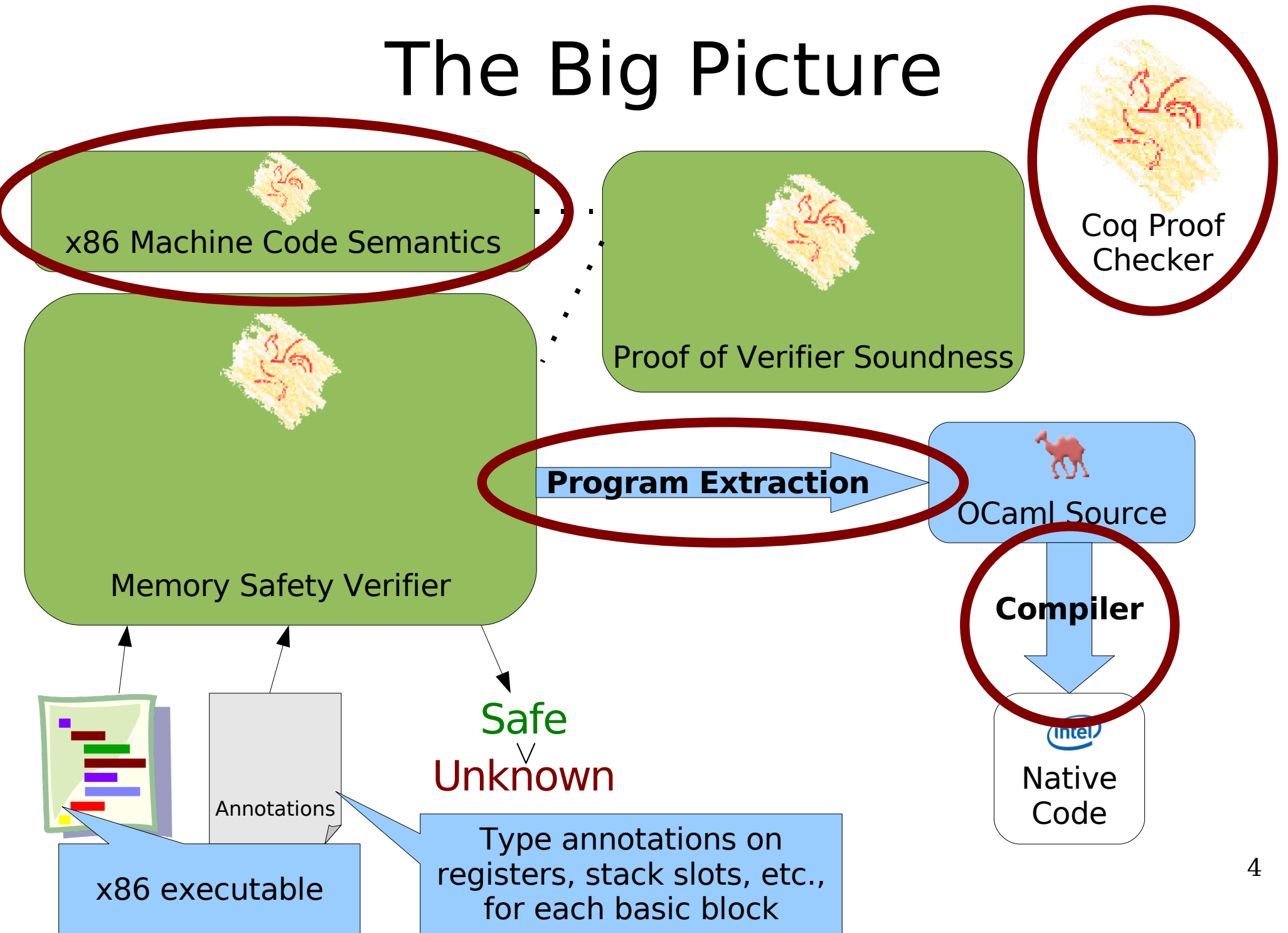
- Proofs about the real machine semantics, written in a very general language
- Proofs are much **larger**, making them expensive to check and transmit



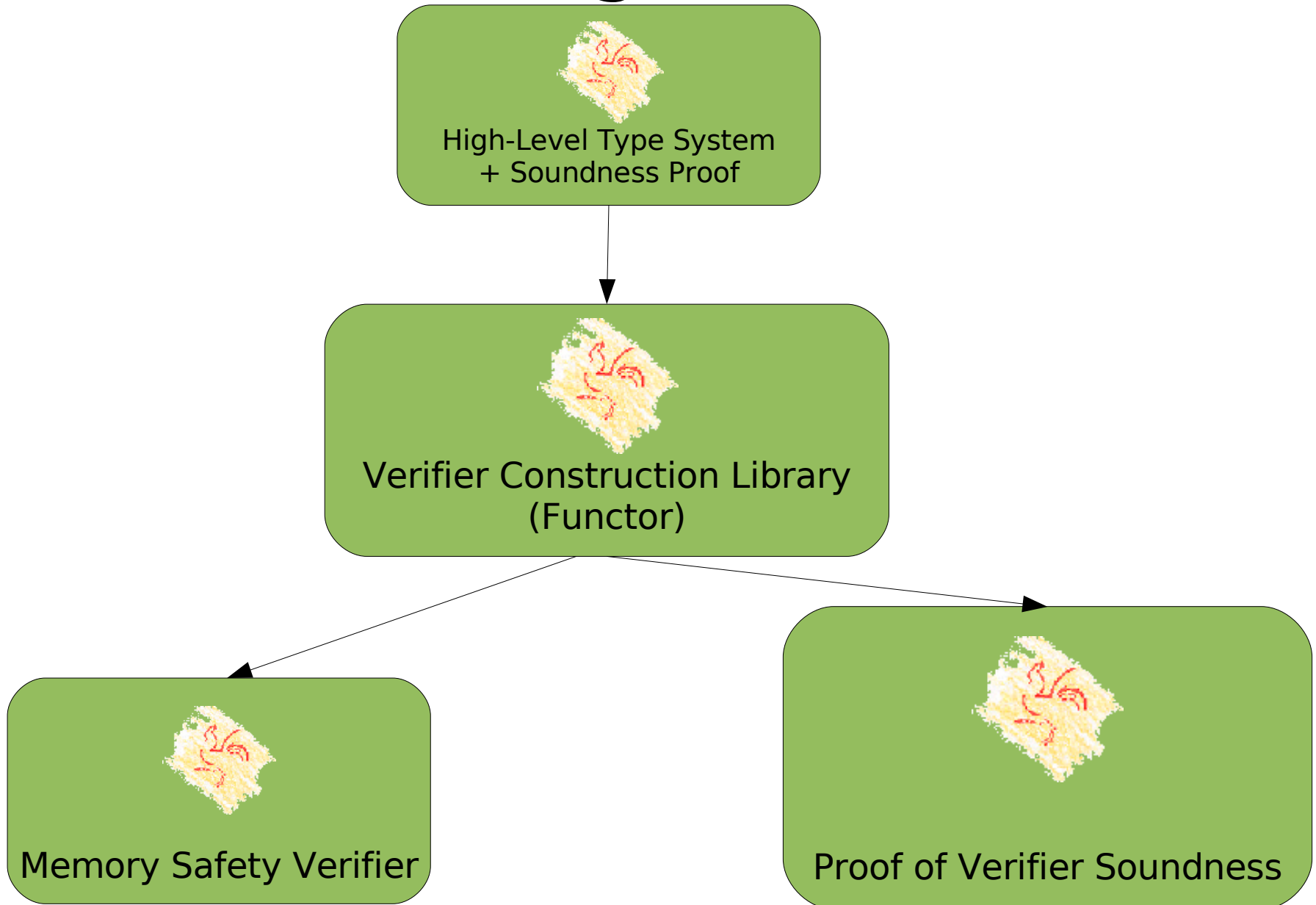
Certified Program Verifiers

- Allow custom executable verifiers that can be **reused**
- Require that every verifier be **proved sound**
- **No proofs** generated or checked at runtime

The Big Picture



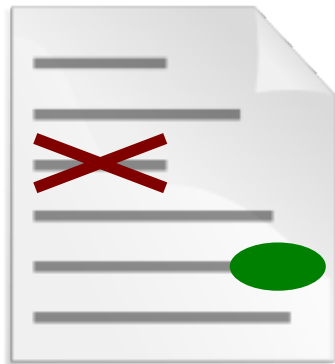
The Big Picture



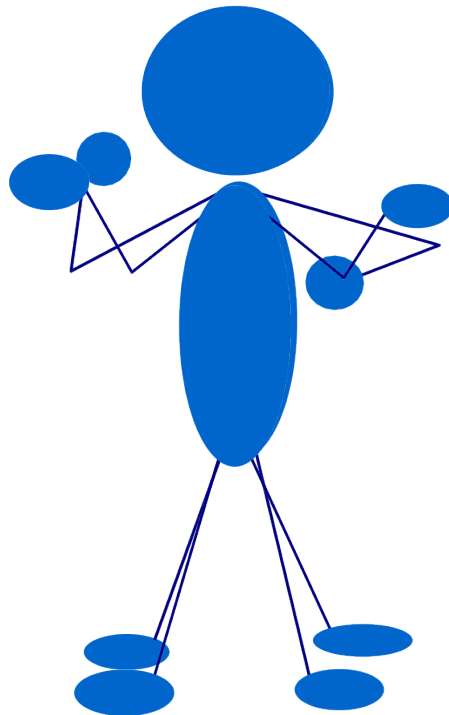
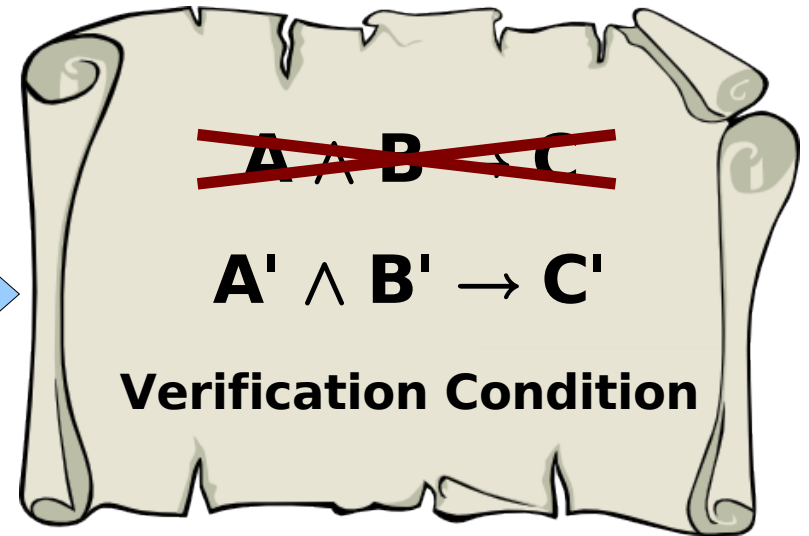
Outline

- Programming with dependent types
 - ...using a proof assistant
- A library for constructing certified verifiers
- Implementation

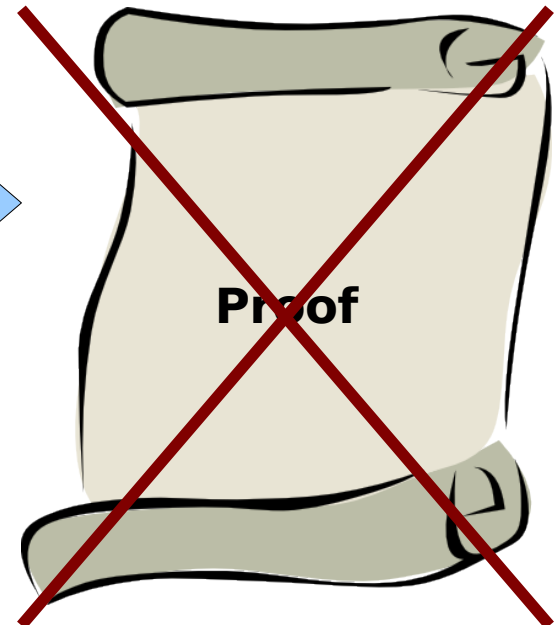
Classical Program Verification



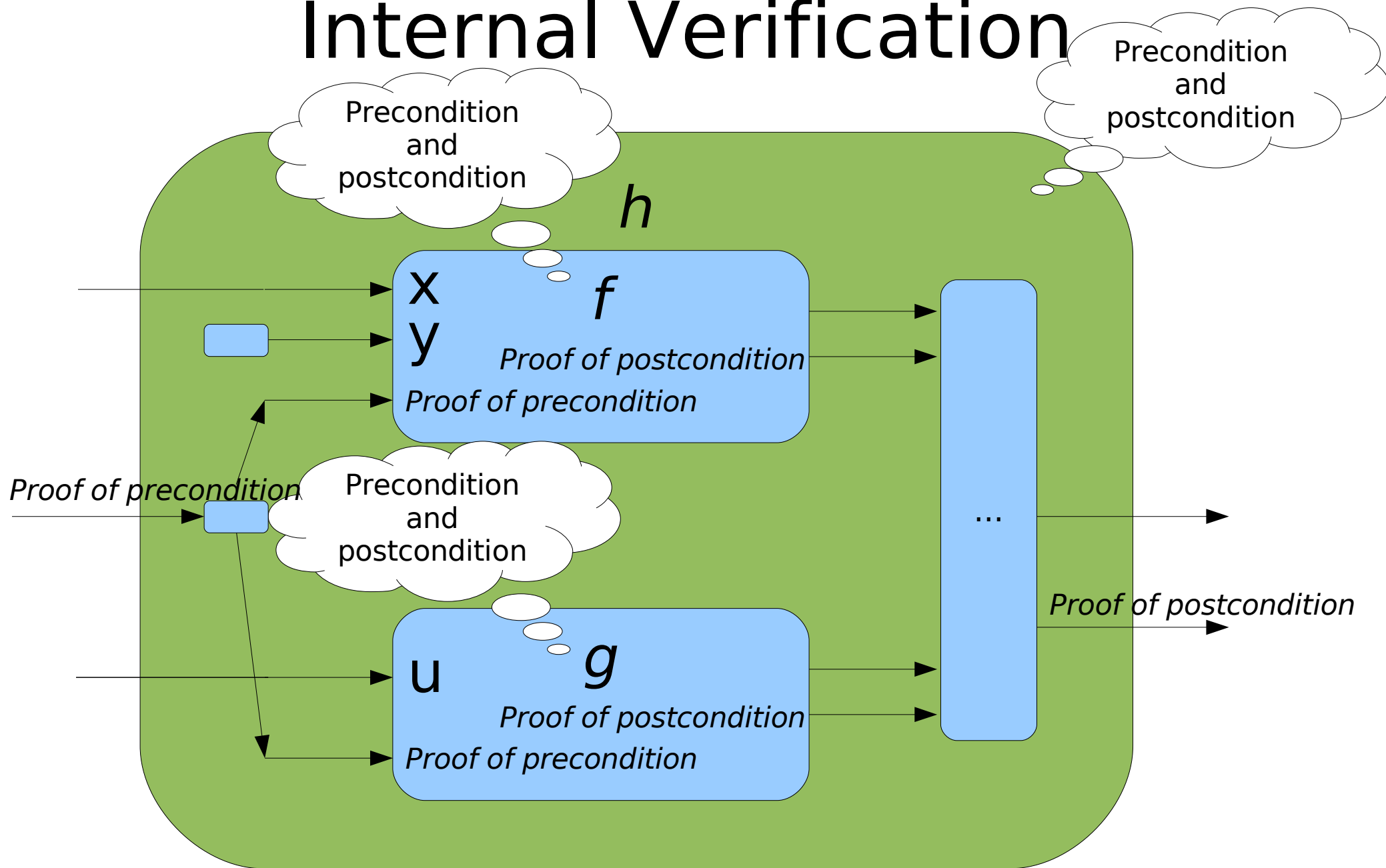
**Verification Condition
Generator**



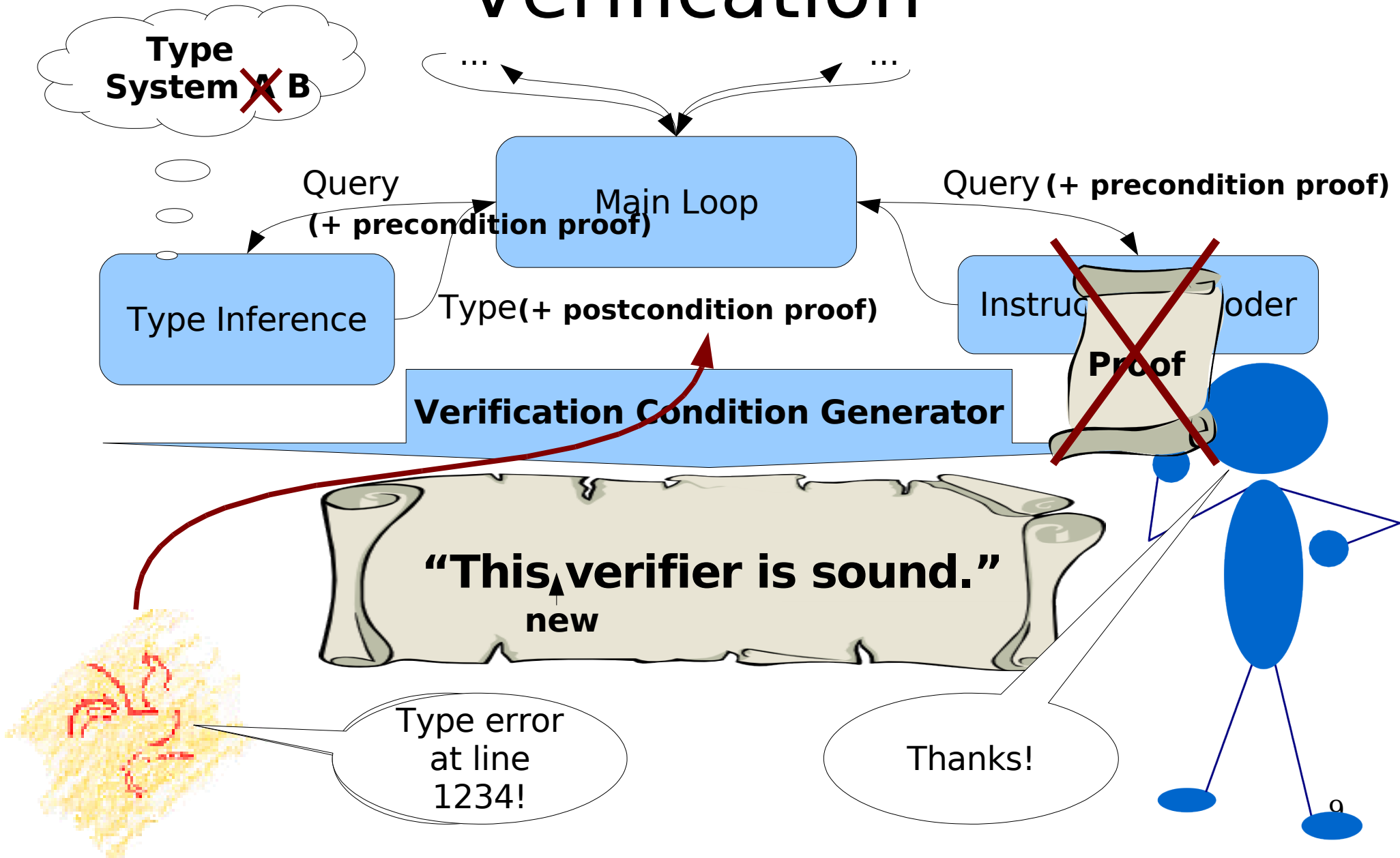
Interactive Provers
(Coq, Isabelle, PVS, etc.)



Internal Verification

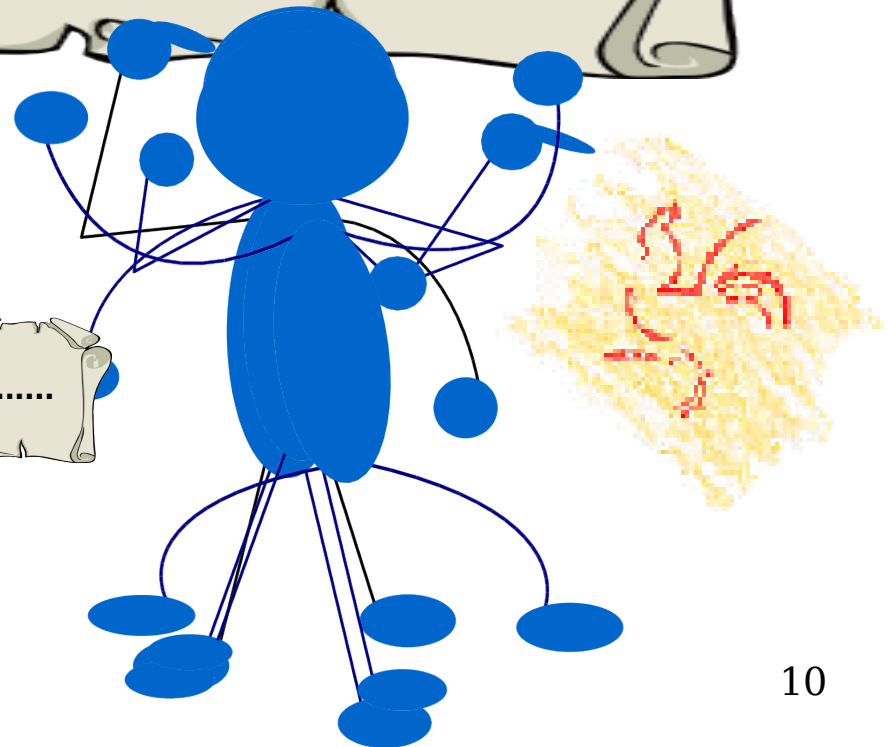
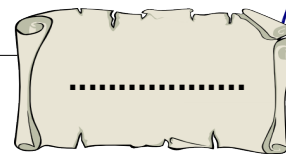
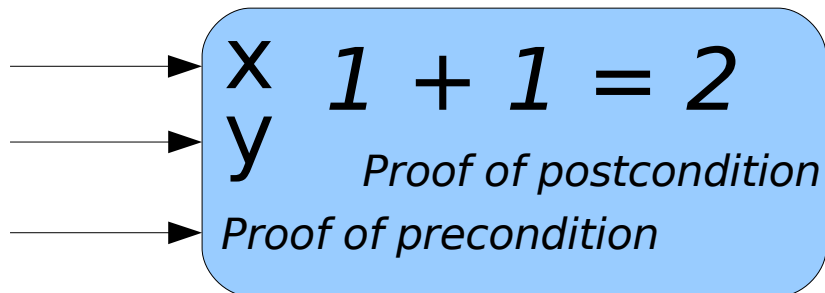


Benefits vs. Classical Verification



Dealing with Proof Terms

```
fun ls1 : list =>
  list_ind
  (fun ls2 : list =>
    forall ls3 ls4 : list,
      append (append ls2 ls3) ls4 = append ls2 (append ls3 ls4))
  (fun ls2 ls3 : list => refl_equal (append ls2 ls3))
  (fun (n : nat) (ls2 : list)
    (IHls1 : forall ls3 ls4 : list,
      append (append ls2 ls3) ls4 = append ls2 (append ls3 ls4))
    (ls3 ls4 : list) =>
    eq_ind_r (fun l : list => cons n l = cons n (append ls2 (append ls3 ls4)))
      (refl_equal (cons n (append ls2 (append ls3 ls4))))
      (IHls1 ls3 ls4)) ls1
```



Mixing Programming with Tactics

```
Definition isEven : forall n, [even(n)].
  refine (fix isEven (n : nat)
    : [even(n)] =
  match n return even(n)
    | 0 -> Yes
    | S 0 ->
    | S (S n)
  proof
  Yes);
auto.
Qed.
```

Step 1. Declare the function

The type of an optional proof of a proposition

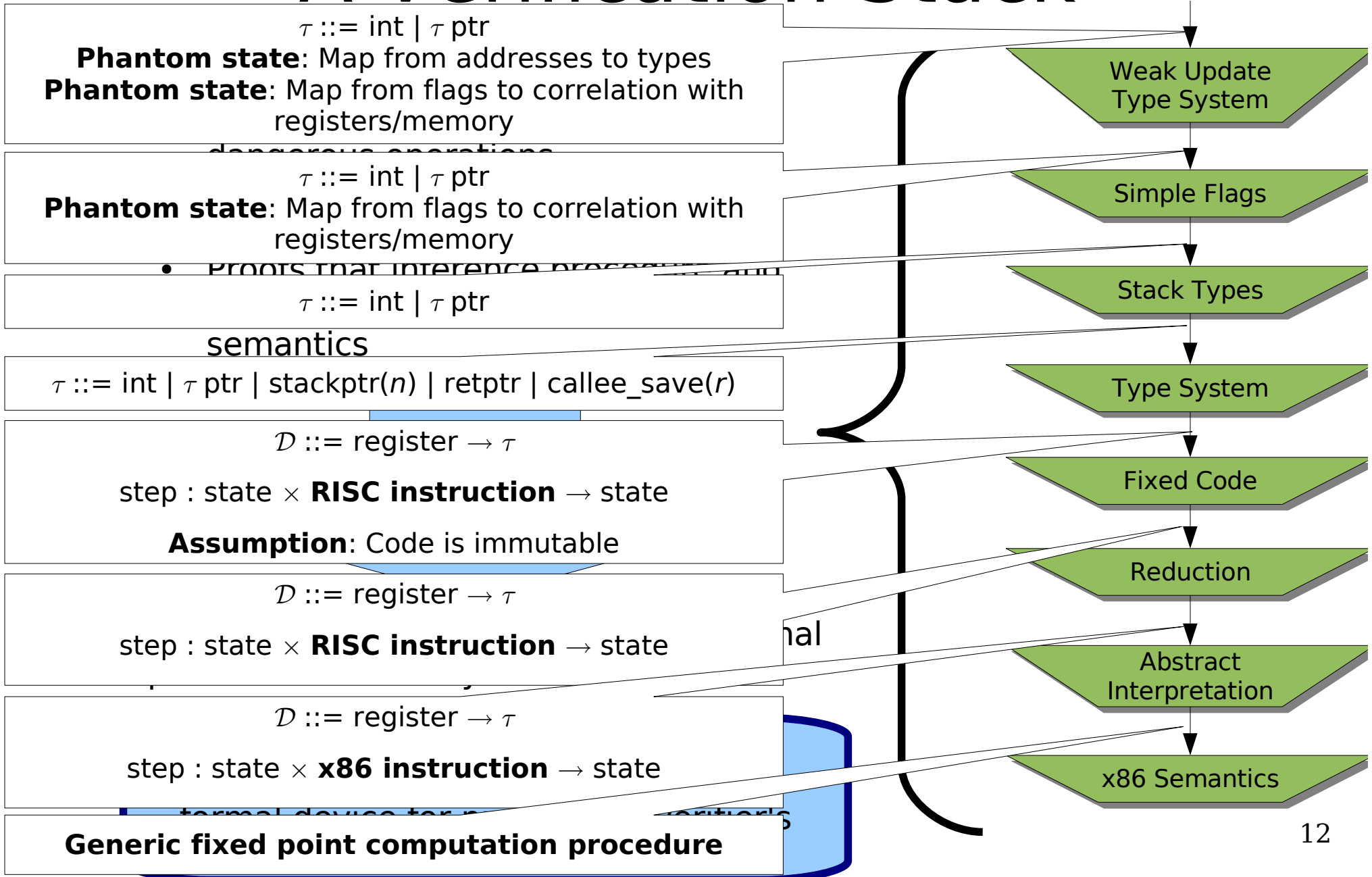
Step 3. Generate the “proof part” of the definition

Generate a proof obligation

Monadic notation: fail if the recursive call fails; otherwise, bind proof in the body.

“proof part” of the definition.

A Verification Stack



Generic fixed point computation procedure

Implementation

Component	Lines of code
Verification stack	7k (Coq)
Bitvectors and fixed-precision arithmetic	1k (Coq)
x86 semantics	1k (Coq)
Utility library	10k (Coq)
x86 binary parser	1500 (OCaml)
New extraction optimizations	1k (OCaml)
Algebraic datatype verifier	600 (Coq)
Total <i>trusted</i>	~5k

Sample Code: Type Language

```
Inductive ty : Set :=
| Constant : int32 -> ty
| Product   : product -> ty
| Sum       : ty -> ty -> ty
| Var       : var -> ty
| Recursive : var -> ty -> ty

with product : Set :=
| PNil : product
| PCons : ty -> product -> product.
```

Sample Code: Subtype Checker

```
Definition subTy : forall (t1 t2 : ty),
  poption (forall ctx v,
    hasTy ctx v t1 -> hasTy ctx v t2).
refine (fix subTy (t1 t2 : ty) {struct t2}
  : poption (forall ctx v,
    hasTy ctx v t1 -> hasTy ctx v t2) :=
  match (t1, t2) with
  | (Constant n1, Constant n2) =>
    pfEq <- int32_eq n1 n2;
    Yes
  | (Product (PCons (Constant n) (PCons t PNil)),
    Sum t1 t2) =>
    if int32_eq n 0 && ty_eq t t1 then Yes
    else if int32_eq n 1 && ty_eq t t2 then Yes
    else No
  | (Recursive x body, t2) =>
    pfSub <- subTy
      (subst x (Recursive x body) body) t2;
    Yes
  | ...
end); .....
```

Qed.

Related Work

- CompCert certified C compiler project [Leroy et al.]
- Foundational proof checkers with small witnesses [Wu et al.]
- Lots of work on building bytecode verifiers with proof assistants

Conclusion

- Today's technology makes constructing certified verifiers with dependent types feasible
- Good mixture of soundness guarantees, ease of engineering, and runtime efficiency

Code and documentation on the web at:
<http://proofos.sourceforge.net/>